

CHEM 524 Course Outline (Sect. 4) – 2013

For html Version of This Set of Notes with Linked Figures from 2005 [CLICK HERE](#)

[Text: Chapter 3, Sect 1 and 4,5](#) directly relates to lecture, in good depth – optics do not change

III. Optics — Control of light — goal: move radiation from the source to the detector in a controlled manner through the experiment

A. Lenses + Mirror (Text: Ch 3 & 1,4) design — shape & materials — efficiency

1. Basic concepts:

index of refraction — $n = c/v$, $c = 3 \times 10^8$ m/s, in a material, the speed of light is reduced $< c$

$n_{CaF_2} \sim 1.35$, $n_{ZnSe} \sim 2.5$, $n_{Ge} \sim 4$ ($n_{fus.qtz} \sim 1.458$, glass: crown ~ 1.57 , flint ~ 1.65 , pyrex ~ 1.47)

[silicates: crown - $\sim 10\%$ KO or other oxides, flint - original had PbO, now TiO or ZrO, pyrex - B_2O_3]

– index goes up with absorbance and delocalization of electrons (heavy atoms, π -systems)

– liquids as well: $n_{water} \sim 1.33$, $n_{alcohol} \sim 1.36$, $n_{CCl_4} \sim 1.466$, $n_{Br-naphthalene} \sim 1.659$

non-isotropic (bi-refringence) depends on direction:

quartz (SiO_2): $n_o \sim 1.544$ $n_e \sim 1.553$, calcite ($CaCO_3$): $n_o \sim 1.6557$ $n_e \sim 1.4852$, zircon ($ZrSiO_4$): $n_o \sim 1.923$ $n_e \sim 1.968$, MgF_2 : $n_o \sim 1.390$ $n_e \sim 1.378$, TiO_2 : $n_o \sim 2.583$ $n_e \sim 2.865$

CdS: $n_o \sim 2.281$ $n_e \sim 2.297$, **CdSe**: $n_o \sim 2.46$ $n_e \sim 2.48$ ($\lambda = 2.5 \mu m$)

(*uniaxial* crystals, o = ordinary, xx and yy, e = extraordinary, zz) – contrast cubic xtal only n

conservation law: $\rho(\lambda) + \alpha(\lambda) + T(\lambda) = 1$ – (do not lose light) mirror $T \sim 0$ & lens $T \sim 1$

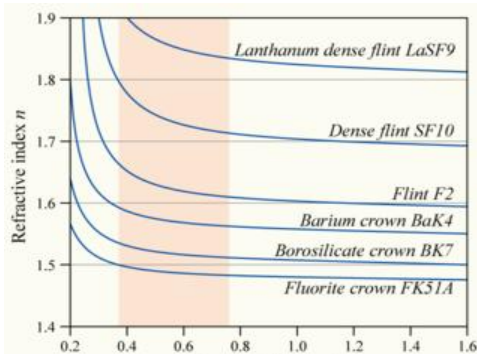
dispersion (index, n, short λ , increase with decrease in λ)

— $dn(\lambda)/d\lambda < 0$ -- bend light by color

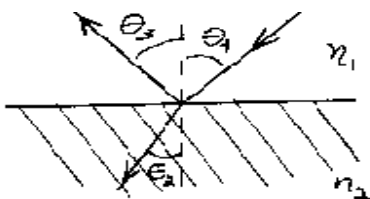
(typical: decrease with increased wavelength λ ,

exception, if absorption band, index is complex and

has singularity, derivative shape, $-/+$ as inc. λ)



Snell's law of refraction: $n_1 \sin \theta_1 = n_2 \sin \theta_2$,



$\theta_1 = \theta_3$ - specular reflection

$\theta_2 < \theta_1$ if $n_1 < n_2$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

normal reflection loss:

$$R(\lambda) = \left(\frac{n_2 - n_1}{n_2 + n_1} \right)^2 = \left(\frac{n - 1}{n + 1} \right)^2$$

$$n = \frac{n_2}{n_1} = \frac{\sin \theta_1}{\sin \theta_2} \quad (\text{Fresnel})$$

$$n = \frac{c}{v} = \sqrt{\frac{\epsilon_r \mu_r}{\epsilon_0 \mu_0}} = \sqrt{\epsilon_r \mu_r}$$

$\epsilon_r \sim$ dielectric constant

$\mu_r \sim$ relative permeability ~ 1

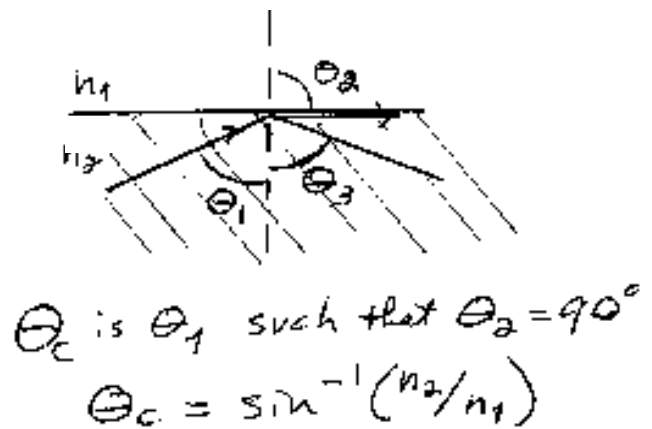
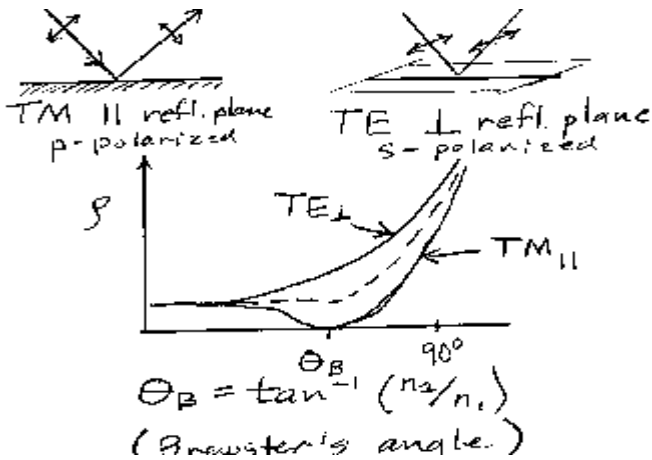
reflection: $\theta_1 = \theta_3$ vs. refraction: $\theta_2 < \theta_1$ for $n_1 < n_2$ – low \rightarrow high, beam toward normal

reflection loss: $\rho(\lambda) = (n_2 - n_1)^2 / (n_2 + n_1)^2$, normal incidence, *more at angle* (window \rightarrow mirror)
 e.g. air/glass $\sim 4\%$ - i.e. $[(1.5 - 1.0)^2 / (1.5 + 1.0)^2 \sim 0.2^2 = 0.04]$, but ZnSe $\sim 18\%$ per surface

Brewster angle, — zero reflection loss in one polarization (|| to reflection plane)

at specific angle $\theta_B = \tan^{-1}(n_2/n_1)$ - other polarization, *|| surface, always some loss*

general: transmit plus reflection, due to interface, always loss, but also *shift polarization*



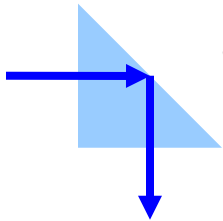
ex: **Brewster** - *air-glass*: $\tan^{-1}(1.5/1) = 56.3^\circ = \theta_B$

- note: θ_B most useful for $n_2 > n_1$

Critical angle: $\sin^{-1}(1.0/1.5) = 41.8^\circ = \theta_c$

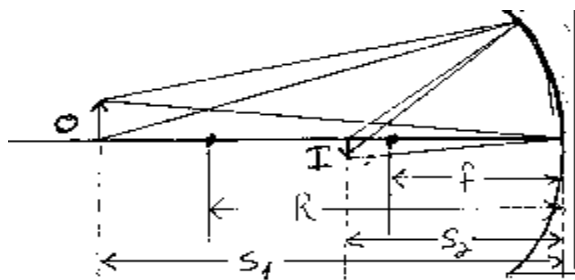
but θ_c only for $n_1 > n_2$

Total internal reflection, - critical angle - **for $n_1 > n_2$** , $\rho(\lambda)$ max at $\theta_1 = \theta_c$, $\theta_c = \sin^{-1}(n_2/n_1)$



air — glass (or quartz), $\theta_c \sim 42^\circ$, useful property for prism reflectors
 (no coating, higher power possible — useful for *steering laser beams*)
 example: $\theta \sim 45^\circ > 42^\circ$ so no transmission, all reflected, *no coating*
 but beam must be collimated, or controlled, since angle $> 42^\circ$

2. Mirrors: spherical mirror imaging — reflection,



$$1/S_1 + 1/S_2 = -2/R = 1/f$$

$R < 0$ - concave

$$m = -I/O = -S_2/S_1$$

spherical mirror focusing - *mirror formula*: **$-2/R = 1/S_1 + 1/S_2 = 1/f$**

S_1 — object — O, S_2 — image — I (+ if O side), R — radius ($R < 0$ concave), f — focus

Ex.: $S_1 = \text{infinite}$, parallel beam, $\rightarrow S_2 = f$ or $S_1 = S_2 = -R \rightarrow 1:1$ imaging

magnification: **$m = -I/O = -S_2/S_1$** compute where place O to get I of different size, (-) *means flip I*:

result: **$S_1 > R$** — demagnify, **$f < S_1 < R$** — magnify, **$S_1 < f$** — no image (diverging beam)

[materials](#) — typically on a glass substrate (stable) or metal for cooling, ground flat or for focus

coating: Al (uv), Ag (vis), Au (IR), overcoating increases ρ , VUV \rightarrow MgF₂, vis \rightarrow SiO, TiO

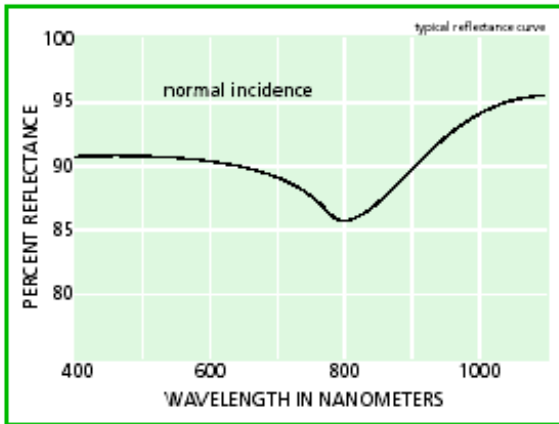


Figure 5.32 Aluminum coating /016

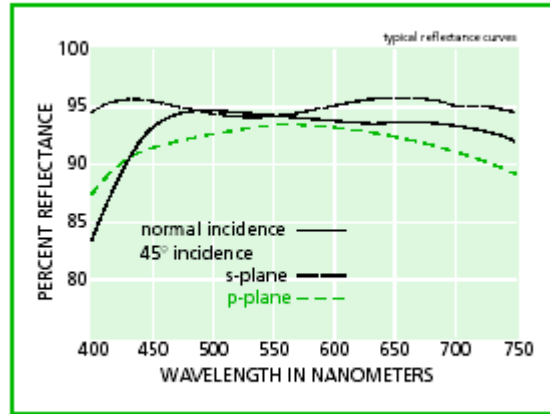


Figure 5.34 Enhanced aluminum coating /023

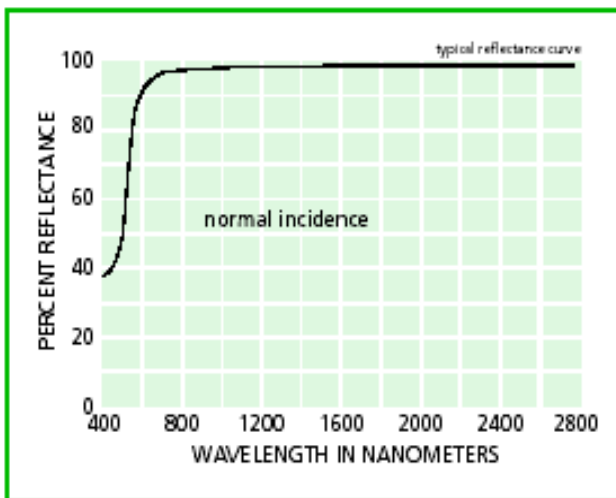


Figure 5.38 Bare gold coating /045

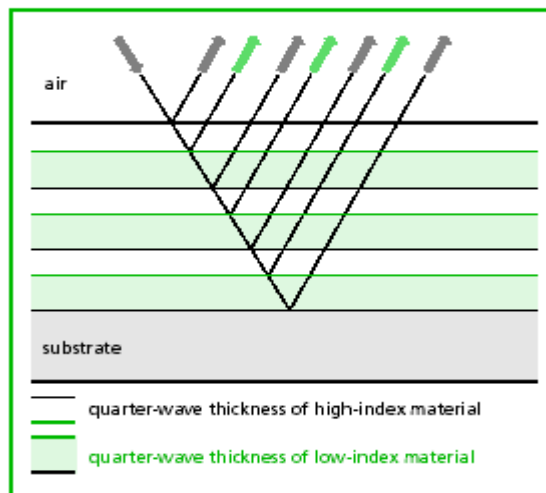
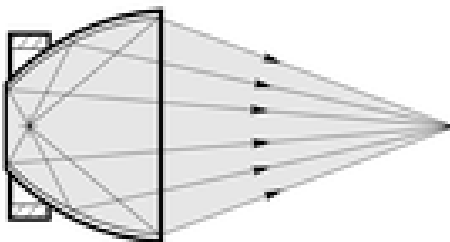


Figure 5.31 A simple quarter-wave stack

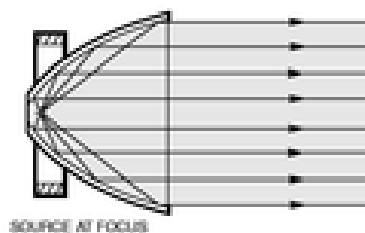
Multilayer dielectric can cause interference ($\lambda/4$ reflection out of phase, $\lambda/2$ – in phase- increase ρ)

vapor deposit oxides (high n) and fluorides (low n) to get layer effect and internal reflect

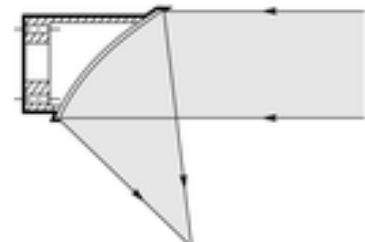
variations: plane, convex (virtual positive image), aspherical, [elliptical](#), [parabolic](#), [off-axis parabola](#)



ellipsoidal –refocus

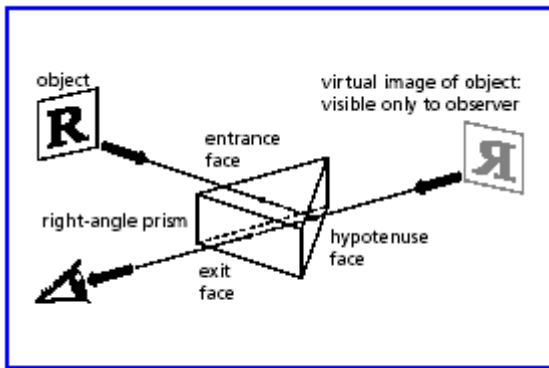


paraboloidal – parallel beam

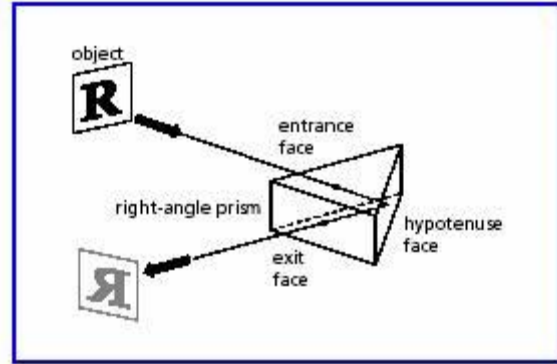


off axis segment

Plane mirror has *virtual image*, $m = 1$, also for Prism—internal reflection, no coating, high power

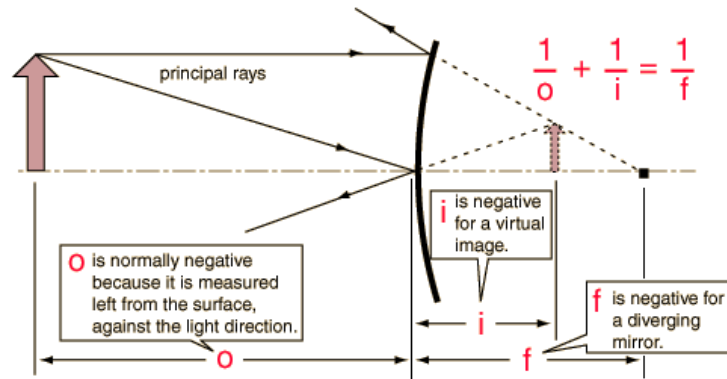
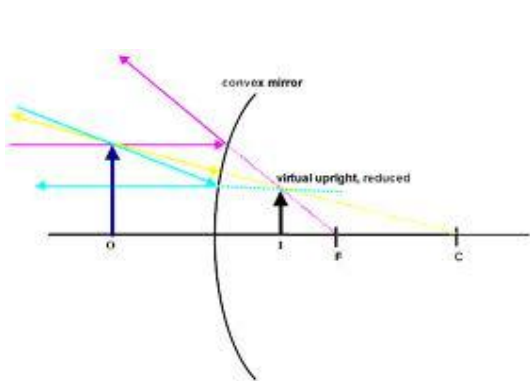


Virtual imaging using a prism



Real imaging using a prism

convex mirror also virtual image but $m (+)$, light diverge from source (object)

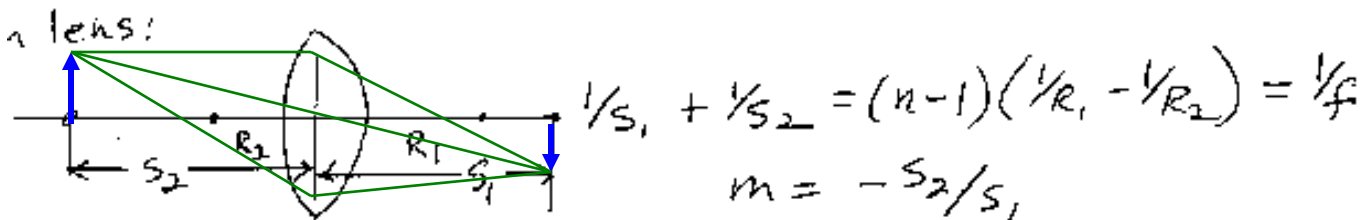


3. Lens: refraction - straight line design, must transmit but losses due reflection or absorption

usable spectral region and focusing range are material and index dependent:

- quartz — uv (180 nm) to near IR $\sim 3 \mu - 4.5 \mu$ (note absorption band at $\sim 4 \mu \sim 2500 \text{ cm}^{-1}$)
- CaF_2 — vuv (140+ nm) to mid IR $\sim 8 \mu$ -- (BaF_2 goes out to $\sim 12 \mu$, vuv, $\sim 160+$ nm)
- ZnSe — yellow (~ 500 nm) to IR $\sim 16 \mu$ -- ($\text{KRS5} - \text{ThBr}_x\text{I}_y$ mix – red, ~ 700 nm, to $\sim 25 \mu$)
- Ge — near IR ($\sim 2 \mu$) to IR $\sim 20 \mu$ -- (Si less range ~ 1.3 to $\sim 16 \mu$)

Thin-lens model, assume thickness not distort, approximation

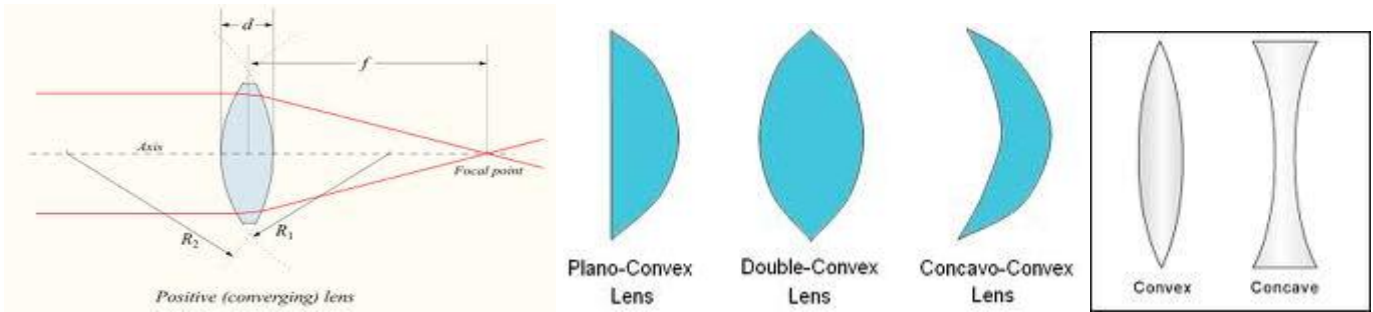


operative formula: $\boxed{1/S_1 + 1/S_2 = 1/f}$, from lens makers formula (above)

lens makers formula for one surface: $n_1/S_1 + n_2/S_2 = (n_2 - n_1)/R$, where R is radius of curve

but, typically purchase based on size, focal length, material → *in practice ignore radius*,
 but can increase efficiency by choosing best combination

magnification: same as mirror: $m = -S_2/S_1$



special designs: cylindrical (focus 1 dim.), aspherical (reduce aberration), doublets etc. (achromat)

AR coating — reduce reflection loss (n — index lens, $n \approx 1$ air) - $\rho = (n-1/n+1)^2$

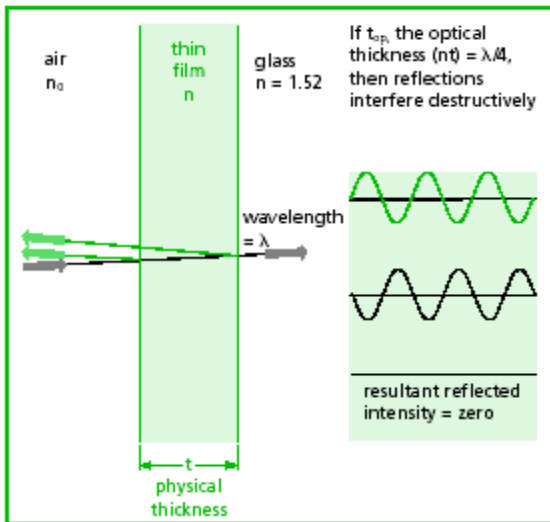


Figure 5.9 Schematic representation of a single-layer antireflection coating

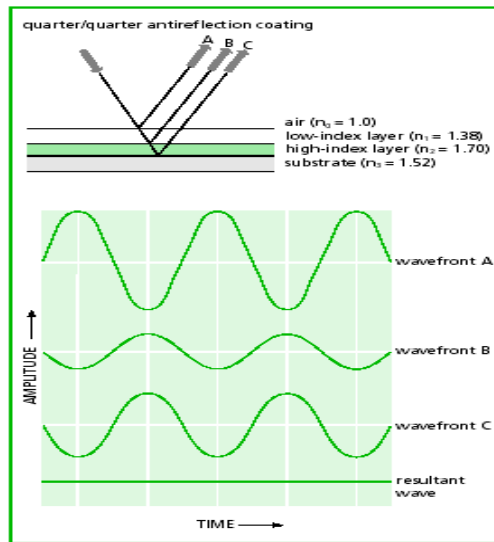
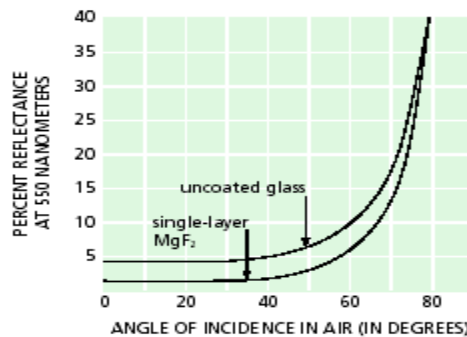
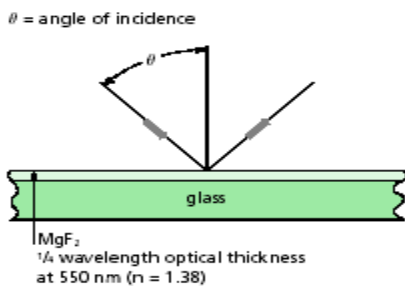


Figure 5.14 Interference in a typical quarter/quarter coating

-- add $\lambda/4$ layer — intermediate: $1 < n_1 < n_{sub}$ reflect from 2 surfaces 90° out of phase - destructive
 or multiple layers — broaden λ range, goal: zero-out reflect by interference, angle sensitive



-- multilayer (N) — get zeros at $(N - 1) \lambda$'s — approximate broad band coverage

4. Light gathering power — trade off: more light collect or smaller image spot ($m = 1$ often best):

closer to source → collect more BUT image bigger
 (further, brighter image, smaller spot BUT less light)

F-number: $[F/n] = f/D$, if not circular shape: $D = (4A/\pi)^{1/2}$

Called the speed — smaller F/n is faster – gather more light

Irradiance (goes as square): halve F/n , quadruple light

(e.g. for photography people: $F/1.4$ is twice the light of $F/2.0$)

Varies as solid angle, Ω , $E = B_s(\pi/4)/(F/n)^2$

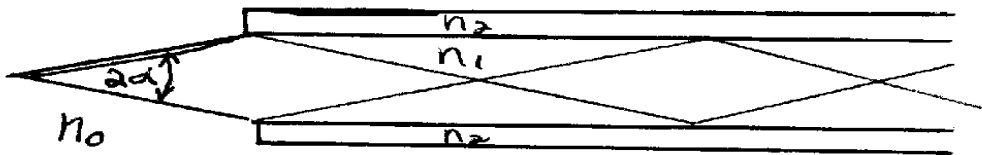
5. Aberrations (solution):

- chromatic (compound lens, mirror),
- spherical (reduce aperture, plano-convex),
- coma (align, reduce aperture),
- astigmatism (reduce off-axis mirror, parabolic)

B. Special

1. Fiber optics — total internal reflection — limits acceptance angle

Fiber Optic — coating cause total internal reflection $n_2 < n_1$



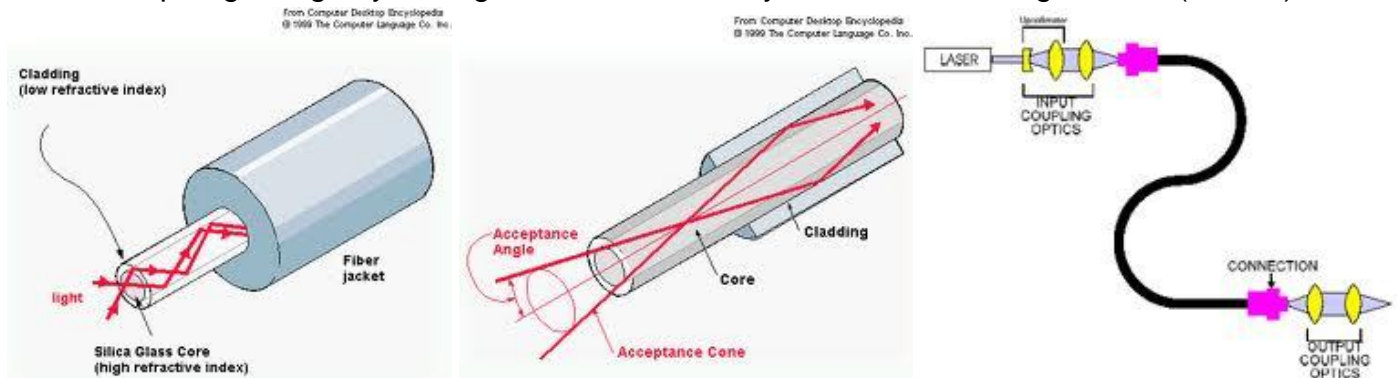
$$\alpha = \sin^{-1} [(n_1^2 - n_2^2)^{1/2}]$$

$$N.A. = n_0 \sin \alpha \sim (n_1^2 - n_2^2)^{1/2}$$

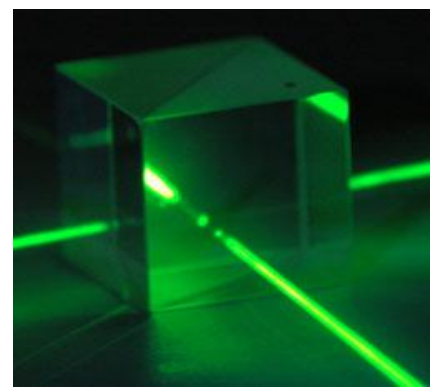
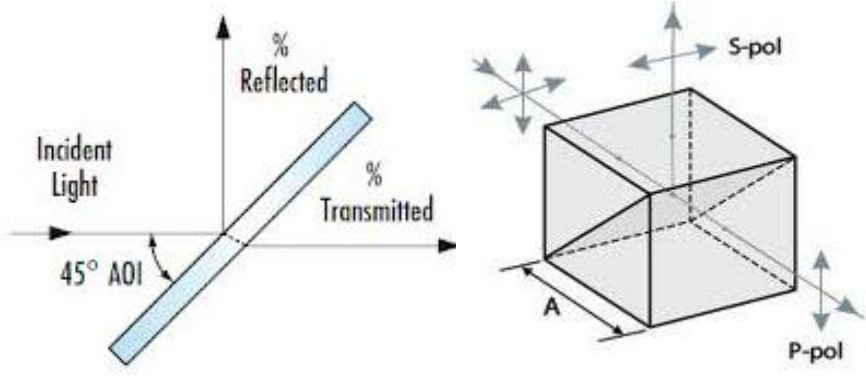
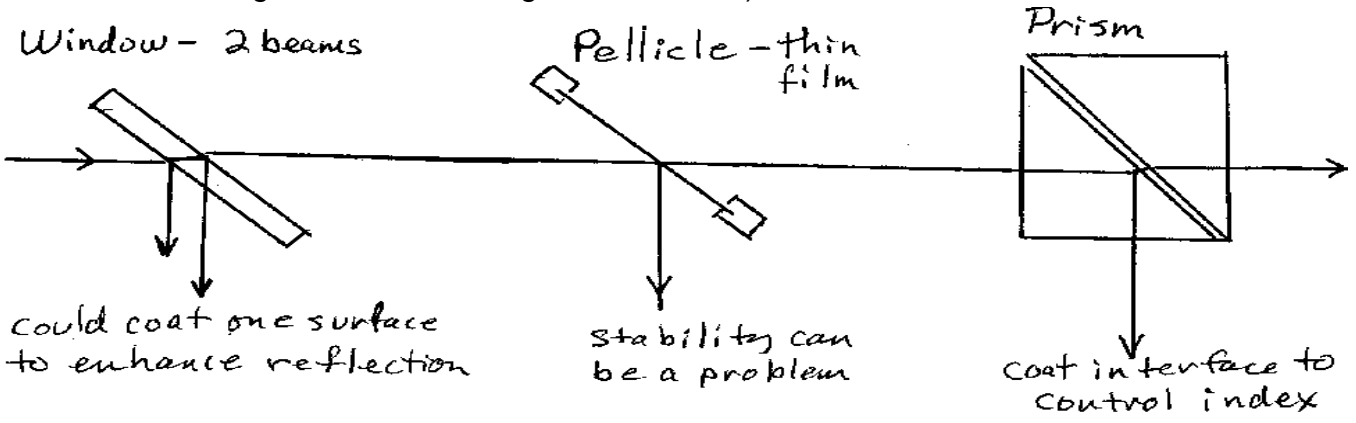
$$F/n = (2 \tan \alpha)^{-1}$$

Important to have **difference in index**, create internal reflection without much loss

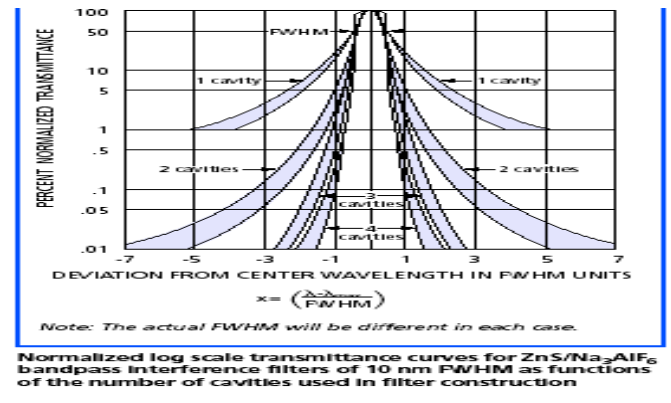
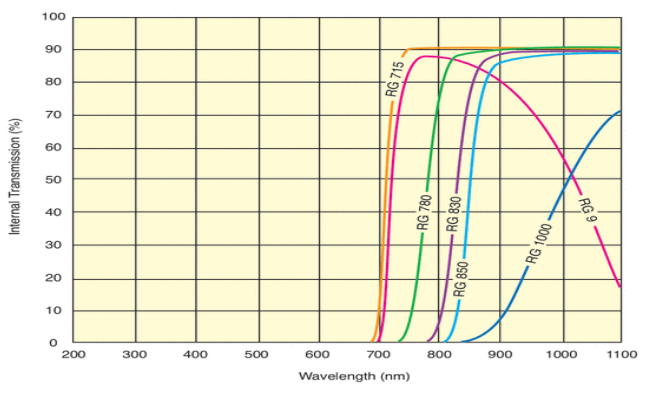
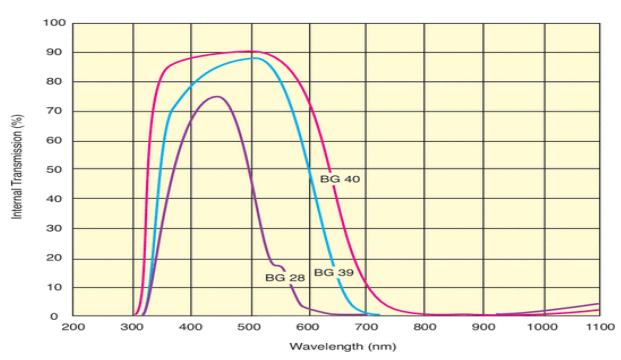
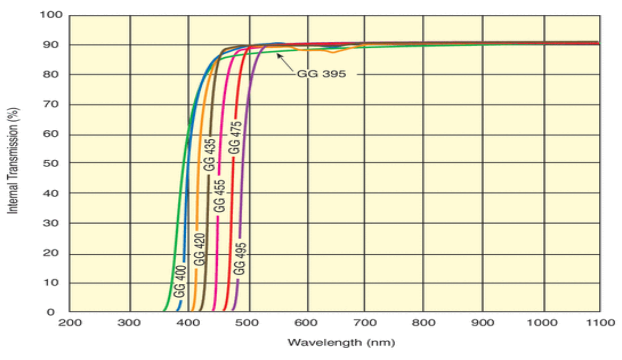
Keep angle large by having **thin fiber** – corollary, harder to insert light beam (bundle)



2. **Beam Splitter** — divides beam in space (can be coating or just surface, can use angle to enhance, single surface best)

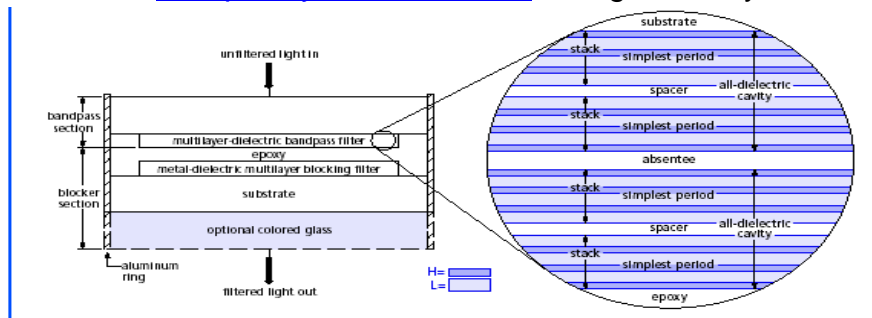


3. **Filters** — color filters are glasses with absorbing materials mixed in, ex. transition metal salts, designed as band pass or cut off, progressing out to even IR, also polymer films with dyes



--interference — narrow -band or cut off available: - constructive interference transmit max:
 $2d(n^2 - \sin^2\theta)^{1/2} = m/\lambda$ where θ is angle of incidence, m is order, d is spacing, n index,
 so can select λ_{max} or angle or spacing depending on material.

create with multiple layers of dielectric acting as Fabry-Perot interferometer,



Microscopes imaging and microsampling have huge impact on modern analytical chem

Simplest would be a magnifying lens, basic idea is to collect light from an object with a fast lens and make an image of it that is bigger.

If view by eye, second (set) lens forms eyepiece to aid in focusing on virtual image at diaphragm

Objective, is the lens or set of lenses that collects light from the object (or specimen)

Characterized by *magnification* (10X, 50X etc.) and *numerical aperture*: $NA = n \sin \alpha$

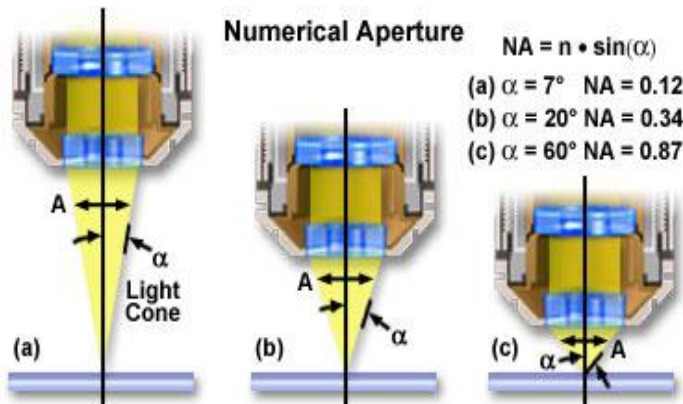


Figure 1

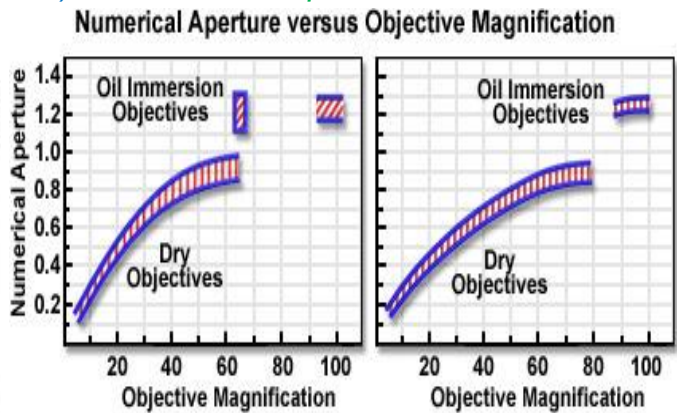


Figure 2

Objective Working and Parfocal Distance



Figure 1

magnification ($m = S_2/S_1$) increase with NA, changing index or add correction can increase NA,

If were simple lens: S_1 would be distance of specimen to objective, effectively the focal length, S_2 "tube length" – design length to focus an image at diaphragm, This is how Olympus defines it, but objective is compound lens, so S_1 seems harder to define, since working distances typically much shorter

Total magnification is product of objective and eyepiece magnifications

Useful range is (500-1000)xNA

Magnification	NA	d (μm)		Corrected Magnification	NA	Typical working distance (mm)	
4x	0.10	2.75		10x	0.45	4.0	
10x	0.20	1.10		20x	0.75	0.35	
20x	0.45	0.69		40x (oil)	1.30	0.20	
40x	0.65	0.42		60x (oil)	1.40	0.21	

Resolution one can get in an image, minimum distance between objects, ideal $\rightarrow d = \lambda/2 NA$

Objects create diffraction patterns, Airy disk, overlap -

shorter λ , higher NA more resolved

NA scale sort of backwards of f/# \rightarrow NA bigger means more light collected

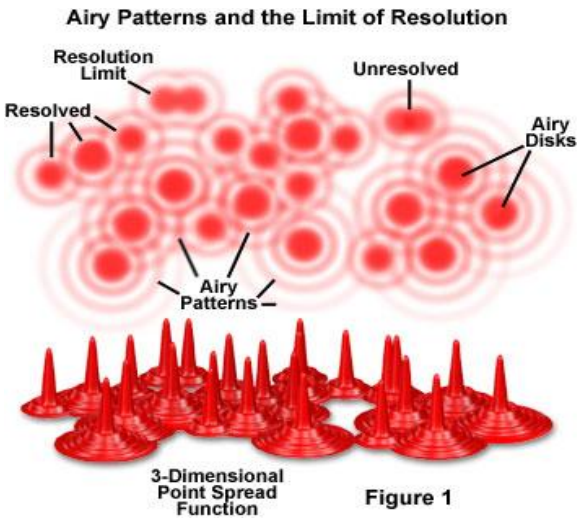
if θ or α is half angle of collection cone, then

$NA = n \sin \theta$ where n is index of medium, for air ~ 1

But if use oil immersion, then $n \sim 1.5$, \rightarrow higher NA

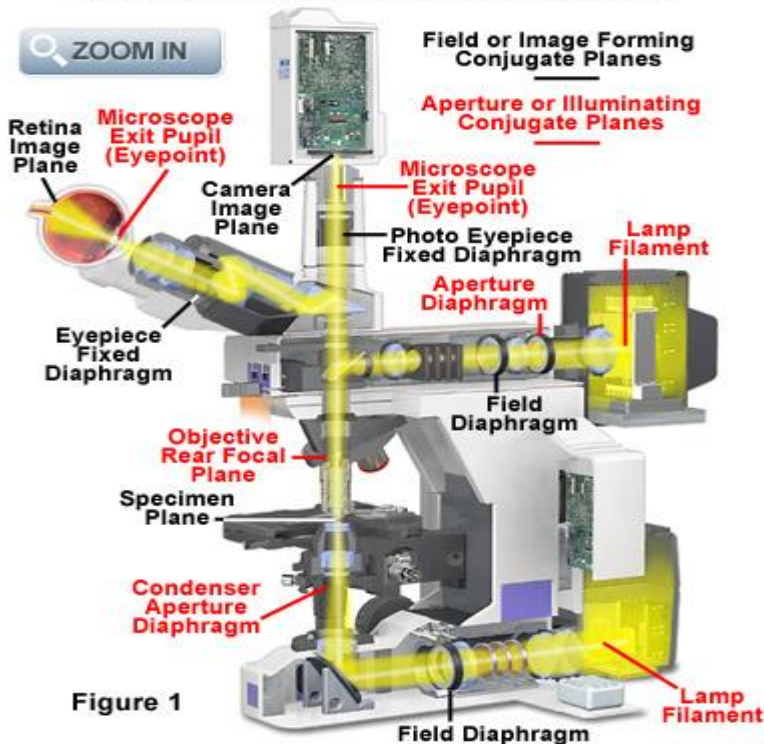
Relation to f/# = f/D for lens \rightarrow

$$NA = n \sin \theta = n \sin [\arctan (D/2f)] \sim nD/2f \sim (n/2)[f/\#]$$

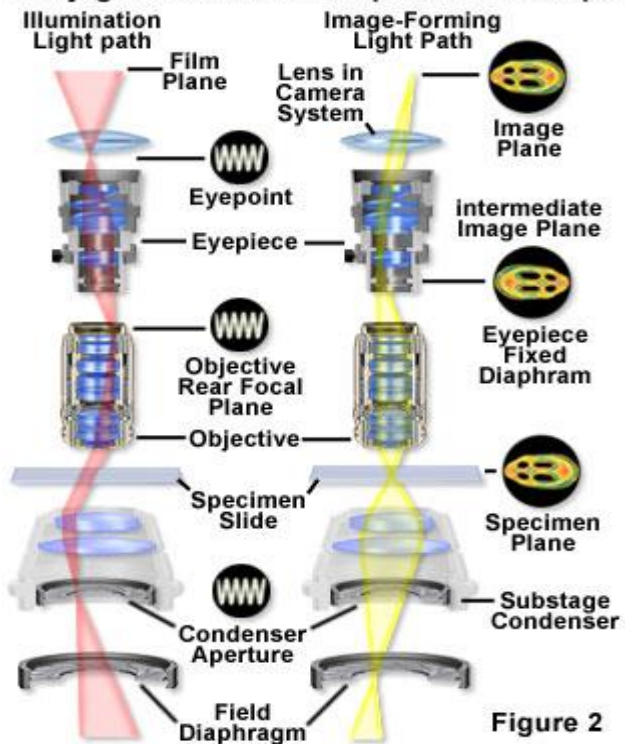


Real microscopes are complex, with multiple lenses, some correct for aberrations, and some act to carry the image to detectors, eye, camera, spectrometer etc.

Conjugate Planes in the Optical Microscope

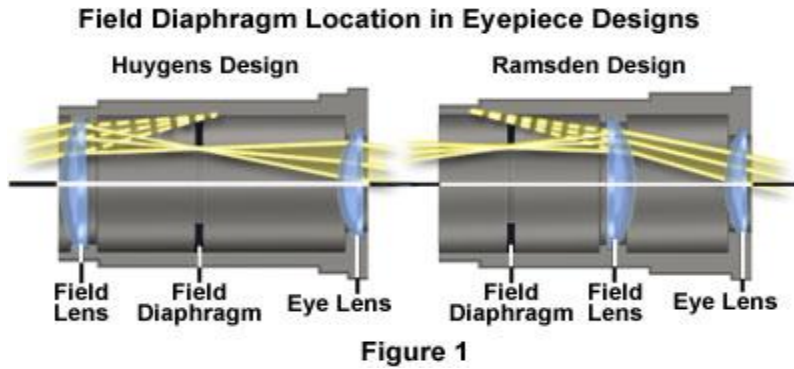


Conjugate Planes in the Optical Microscope



Conjugate planes - about illumination and detection and different planes in which each is in focus

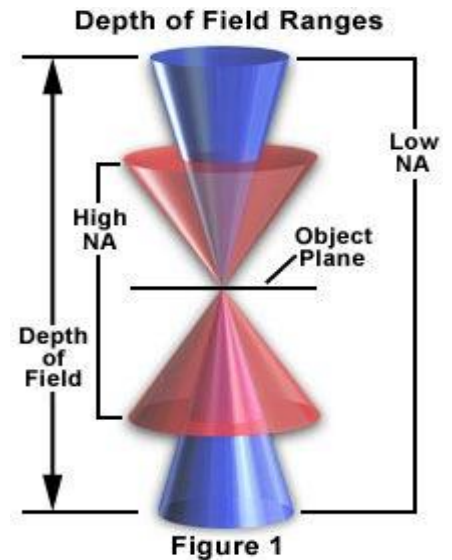
At high magnification, the lens gets very close to the object (specimen) and the properties of the Sample and slide/coverslip can affect resolution in practice due to aberrations
 Traditional objectives focused at 160 mm, so at 40x they would be ~4 mm from the sample
 New ones are designed for infinity imaging, create parallel light, make more room for add-on so an eyepiece refocuses the image, and can add magnification.



Field of view is controlled by the eyepiece and an intermediate field lens,
 $Field = fn/m$ - $m = magnification$
 fn – diameter of view field in image plane,
 field size determined by diameter of diaphragm

Depth of focus (or field) – d.f. controlled by the NA

So can see above and below the specimen plane, tells what parts above and below in focus. If image on a camera or the like, will be seeing effectively one plane, but if doing spectroscopy can get data from some range through sample
 Image is magnified, so has different depth but related

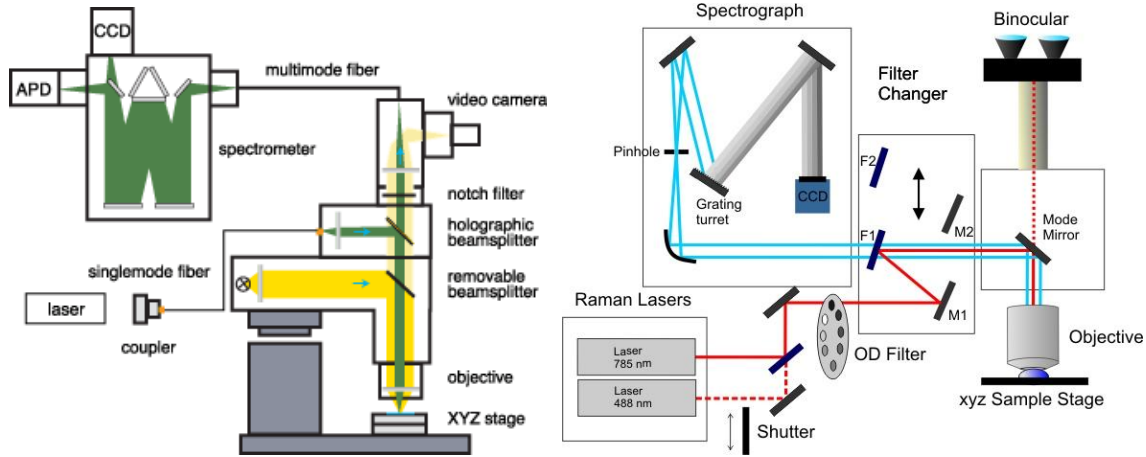


Ex: Magn.	NA	d.f.(μ)	image(mm)
4x	0.10	55.5	0.13
10x	0.25	8.5	0.80
20x	0.40	5.8	3.8

Illumination – since you need light to see an image, much effort has been in illuminator design, idea is not to focus source on specimen but on the aperture of the objective, to create even illumination and no image of the filament, etc.

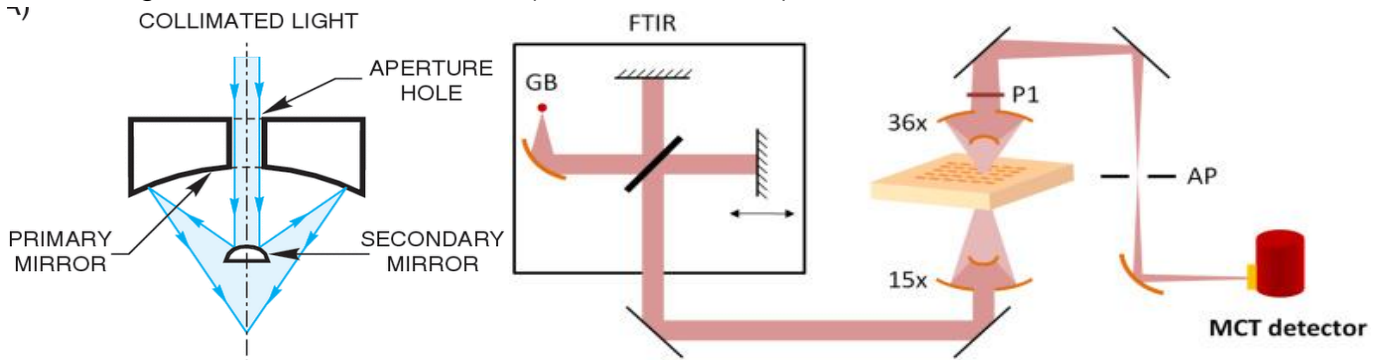
Spectroscopy - the sample is the source, if fluorescence or Raman, which should be evenly excited—or use laser focus to pick out a specific part of sample for spectral analyses—improve resolution over microscope itself. These ideas also useful for absorbance (vis or IR)

Raman or fluorescence Microscopes

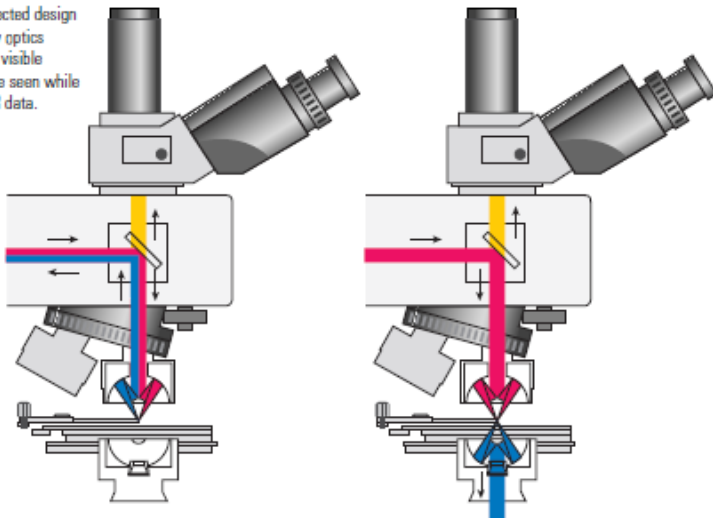


Excitation is often a laser, but now often use non-linear responses to get selectivity and to get enhanced resolution effects as well. Short wavelengths allow resolutions to ~ 500 nm, but bio systems can image parts of cells and thus get information about distribution of species in cell. Using labels in fluorescence can follow bio processes, but they need to be incorporated. Raman is in principle “label free” but often needs substantial sample size, unless tricks are used like SERS.

IR microscopes—problem of absorption of the lenses, so typically use a mirror optic for objective — Cassegrain collector or use ATR (internal reflection)

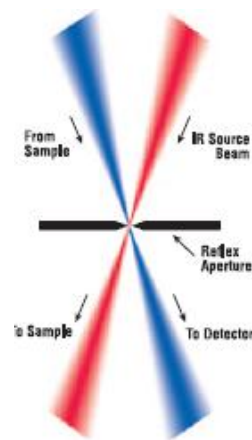


corrected design
view optics
are visible
to be seen while
getting IR data.



Reflection mode

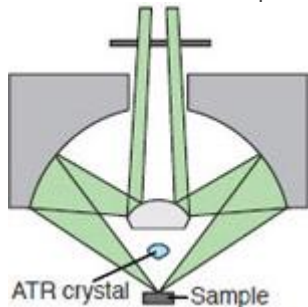
Transmission mode



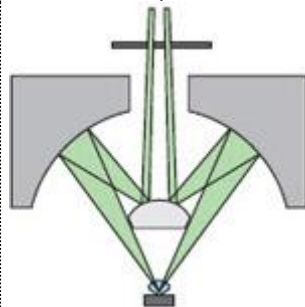
Aperture select part of sample

Big application has become imaging, not just spectroscopy of spot but spatially selective spectra of image, in effect this becomes *chemically edited*. So for materials can see inhomogeneities and identify what they are, for pharma can monitor distributions in formulations of drugs (e.g. tablets, etc), for bio samples can analyze variations in tissue, disease identifications and other biomedical applications. Longer wavelength limits resolution, typically ~5-10 micron.

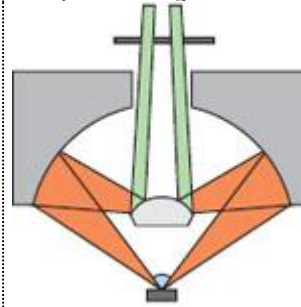
Normal sample view with the crystal element in the raised position



Sample viewing after crystal contact with the sample area



ATR measurement and simultaneous sample viewing



JASCO ATR objective design

Homework, will be part of set #2

- read Chap 3-1, 4, 5 (then 3-2, 3, which carry over to Section 5, Special Optics)
- to discuss: Problem 3-2, 11, 19,

Problems to do: Ch 3: # 2, 7, 10, 11, 13, and

- a. I have a spectrometer that I wish to illuminate. To get the maximum efficiency, I need to image the source on the entrance slit ($100\ \mu \times 5\ \text{mm}$). Only the amount of power incident on the opening of the slit makes it to the detector. To properly use the spectrometer, the incident light should enter with an F/4 cone. You have a quartz halogen lamp (with a filament $1\ \text{mm} \times 10\ \text{mm}$) and three lenses, each $50\ \text{mm}$ in diameter, with focal lengths of 50 , 200 and $1000\ \text{mm}$. What lens do you choose and where do you place it and the source to get the best throughput efficiency at the slit?. Why?
- b. I want to build a sample chamber for microsampling (e.g. ~ 0.1 - $1.0\ \text{mm}$ diam.) using an FTIR spectrometer, to collect spectra in the 3 - $10\ \mu\text{m}$ range. Should I use lenses or mirrors to focus the output of the interferometer on the sample and collect the light again and refocus on the detector (area $1\ \text{mm}^2$)? Why? What kind (size, focal length, material/coating) lenses or mirrors would be needed to create an essentially straight design (i.e. compact) that will match both focusing requirements.

Links to optics etc:

Iowa State course, properties of light (sort of just formulas),
<http://avogadro.chem.iastate.edu/CHEM513/513-1.pdf>
 physicaloptics
<http://avogadro.chem.iastate.edu/CHEM513/513-2.pdf>
<http://avogadro.chem.iastate.edu/CHEM513/513-3.pdf>

Optics companies: (first two, more precision items)

Newport (some tutorial info is contained on specific product pages, like aspheric lenses, etc.)

<http://www.newport.com/Optics/5677806/1033/section.aspx>

Melles-Griot

www.cvimellesgriot.com/Products/Optical-Components.aspx

Edmund Optics

<http://www.edmundoptics.com/onlinecatalog/browse.cfm>

Edmund Scientific, wide variety of lenses and mirrors, originally for astronomy hobbyist

http://scientificsonline.com/category.asp_Q_c_E_424411

American Science Surplus Center—great source for cheap optics

<http://www.sciplus.com/category.cfm?subsection=21>

Mark Optics, CA

<http://markoptics.com/pages/products.htm>

Microscopes:

Nikon and Olympus both have excellent tutorials on microscopy

<http://www.microscopyu.com/articles/formulas/>

<http://www.olympusmicro.com/index.html>